Section 3.6 Mathematics of Finance

Calculating the Amount in an account for Compound Interest Paid *n* times a year

If you deposit P dollars at a rate r (in decimal form) subject to compound interest paid n times a year, then the amount, A, of money in the account after t years is given by

$$A = P \left(1 + \frac{r}{n} \right)^{(nt)}$$

Annually n= ____ Semi-Annually n=____ Quarterly n=____ Monthly n=____ Weekly n=____

Examples:

- 1. You deposit \$1000 in a savings account at a bank that has a rate of 0.95%.
 - a. Find the amount, A, of money in the account after five years, subject to interest compounded annually. Round to the nearest cent.
 - b. Find the interest after five years.
- 2. You deposit \$4200 in a savings account that has a rate of 1.125%. The interest is compounded quarterly.
 - a. How much money will you have after ten years? Round to the nearest cent.
 - b. Find the interest after ten years.
- 3. How much money should be deposited today in an account that earns 7% compounded monthly, so that it will accumulate to \$10,000 in eight years?
- 4. If John invests \$2300 in a savings account with a 9% interest rate compounded quarterly, how long will it take until John's account has a balance of \$4150?
- 5. What interest rate compounded daily (365 days/year) is required for a \$22,000 investment to grow to \$36,500 in 5 years?

Calculating the Amount in an account when Compounding Interest Continuously

If you deposit P dollars at a rate r (in decimal form) and the interest is compounded continuously, then the amount, A, of money in the account after t years is given by

$$A = Pe^{(rt)}$$
 where $e \approx 2.71828$ (use the e^x button on your calculator)

Examples:

6. A single payment of \$10,000 is invested at an annual rate of 8%, compounded continuously. Find the balance in the account after 5 years.

7. You have deposited \$1000 in an account that pays 6.25% interest compounded continuously. How long will it take for your money to double?

- 8. When your initial investment is earning interest in an account with continuous compounding, find the missing information given the various conditions.
- a) Initial Investment: \$12,500 APR 9% Time to double your money? Amount in 15 years?

b) Initial Investment: \$9,500 APR ? Time to double your money: 4 years Amount in 15 years?